

Vulpus Labs

Pow!

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Introduction

Pow! is a simple non-linear voltage-to-voltage converter which applies a power function to the input signal, with a curve that maps 0v to 0v and +5v to +5v while passing through a midpoint (x, y) where $+xV$ is mapped to $+yV$.



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KNOW MANY THINGS

The values of x and y can be set via knobs or by dragging a control point on the display, and can also be modulated by input signals.

For negative voltages (-5v to 0v) either an inverse curve is applied, mapping -5v to -5v and $-xV$ to $-yV$, or the signal is rectified, mapping -5v to +5v and $-xV$ to $+yV$. Scaling and DC bias can also be added post-rectification.

Theory of Operation

Input voltages in the range -5v to +5v are mapped into the numeric range -1 to 1, and transformed with the power function

$$y = |x|^{\frac{\log(mid_y)}{\log(mid_x)}}$$

where ($0.001 \leq mid_x \leq 0.999$, $0.001 \leq mid_y \leq 0.999$) is the midpoint position through which we want the resulting curve to pass.

The alert reader will have noticed that the transformation is really governed by a single exponent $y = |x|^n$, in the range

$$\frac{\log(0.999)}{\log(0.001)} \leq n \leq \frac{\log(0.001)}{\log(0.999)}$$








which is naturally 1 whenever $mid_x = mid_y$.

We could have opted to control this with a single knob and/or CV input. However, having a controllable midpoint means we can combine modulation signals in some interesting ways, where the value of mid_x affects the influence of mid_y on the value of the exponent n (and hence the shape of the curve), and vice versa.

After the power function transform, the resulting value $0 \leq y \leq 1$ is mapped back into the range -5v to +5 in one of three ways:

- **No rectification:** if $x < 0$ return $-5y$, else return $5y$
- **Rectified:** return $5y$
- **Rectified and scaled/bias corrected:** return $10y - 5$

Here are the some examples of the transformations these can produce on a simple sine wave:

	<p>Unrectified, midpoint at (0.5, 0.5), signal is passed through unchanged</p>
	<p>Rectified - lower part of signal is inverted, doubling frequency</p>
	<p>Rectified with DC correction and scaling - rectified signal is boosted 100% and re-centred around 0v</p>
	<p>Unrectified, midpoint at (0.75, 0.5) - sine wave shape is "thinned"</p>
	<p>Unrectified, midpoint at (0.75, 0.5) - sawtooth wave is "non-linearised" (straight lines turn curvy)</p>
	<p>Uncertified, midpoint at (0.5, 0.9) - triangle wave is "fattened" and smoothed out</p>
	<p>Modulating the midX position with a second oscillator to create a more complex waveform</p>

And here is a simple mono instrument with the output of an ADSR envelope generator fed into the midpoint Y control:



Controls



There are three **IN** jacks, **L**, **R** and **POLY**. If only the **L** jack is connected, a mono signal is processed and sent to both the **L** and **R** output jacks. If both **L** and **R** are connected, a stereo signal is processed. If **POLY** is connected, then all active polyphonic channels in the input are processed and sent to the **POLY** output jack.

The curve display shows the shape of the curve, with the midpoint marked out with a small circle. Click anywhere within the display to move the midpoint to that point.

The midpoint is also controlled with the **MID POINT X** and **Y** knobs. These can also be modulated by a CV signal connected to the **MOD IN X** and **Y** jacks, with the **MOD AMT X** and **Y** knob controlling how much the CV signal affects the midpoint.

The **RECTIFICATION** knob selects the rectification mode (*left* = no rectification, *middle* = rectified, *right* = rectified and scaled / bias corrected).

Take outputs from the **OUT** section at the bottom.

Credits and Acknowledgements

Pow! was written by Dominic Fox in October 2024.

Thanks to the developers at Cherry Audio for their great products, especially Voltage Modular.